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► To cite this version:

Clément Mallet, Florent Lafarge, Frédéric Bretar, Uwe Soergel, Christian Heipke. LIDAR WAVEFORM MODELING USING A MARKED POINT PROCESS. International Conference on Image Processing (ICIP), Nov 2009, Cairo, Egypt. hal-00781804

HAL Id: hal-00781804

<https://inria.hal.science/hal-00781804>

Submitted on 28 Jan 2013

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LIDAR WAVEFORM MODELING USING A MARKED POINT PROCESS

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ABSTRACT

Lidar waveforms are 1D signal consisting of a train of echoes where each of them correspond to a scattering target of the Earth surface. Modeling these echoes with the appropriate parametric function is necessary to retrieve physical information about these objects and characterize their properties. This paper presents a marked point process based model to reconstruct a lidar signal in terms of a set of parametric functions. The model takes into account both a data term which measures the coherence between the models and the waveforms, and a regularizing term which introduces physical knowledge on the reconstructed signal. We search for the best configuration of functions by performing a Reversible Jump Markov Chain Monte Carlo sampler coupled with a simulated annealing. Results are finally presented on different kinds of signals in urban areas.

Index Terms— Signal reconstruction, Lidar, Source modeling, Marked point process, RJMCMC, 3D point cloud.

1. INTRODUCTION

Airborne laser scanning is an active remote sensing technique providing range data as georeferenced 3D point clouds. It enables fast, reliable, accurate, but irregular mapping of both terrain and elevated features such as the tree canopy and the ground underneath. The new technology of full-waveform lidar systems permits to record the backscattered signal for each transmitted laser pulse (*i.e.*, an intensity histogram). Instead of clouds of individual 3D points, lidar devices provide connected 1D profiles of the 3D scene, which contain more detailed information about the structure of the illuminated surfaces [1]. Indeed, each signal consists of series of temporal modes (called *echoes*), where each of them corresponds to an individual reflection from an object (see Figure 1).

Thus, the decomposition of the waveforms allows first to find the

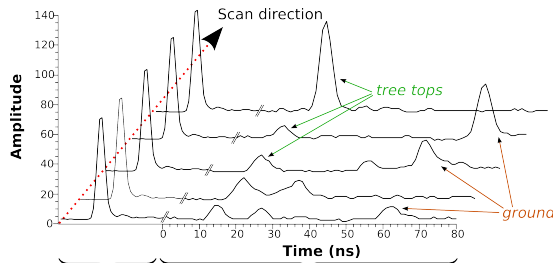


Fig. 1. Example of consecutive lidar waveforms.

3D location of the targets. Besides, modeling each echo with a suitable analytical function permits to retrieve its shape, which can provide relevant features for segmentation/classification algorithms

[2]. Lidar signal reconstruction is then a topic of major interest.

The conventional methods for reconstructing 1D signals such as wavelets, splines [3] or Gaussian mixture models [4] are not particularly adapted since they are too general, do not always model each mode of the waveform and do not take into account the physical characteristics of lidar waveforms. Some specific lidar algorithms have been proposed using for instance the non-linear least-square approach [5]. However, the gradient computation required in such models limits both the introduction of physical knowledge on the waveforms and the type of the chosen function.

Stochastic approaches based on marked point processes [6] are very promising for addressing the issue of reconstructing lidar waveforms. These models have shown good potentialities for many applications in image analysis such as the extraction of road network [7], vascular trees [8] or 3D urban objects [9]. Our method simulates mixtures of various parametric functions representing the reconstructed echos. An energy is associated to each configuration and the global minimum is then found using a Reversible Jump Markov Chain Monte Carlo (RJMCMC) algorithm [10]. Our model presents several interesting characteristics compared to conventional waveform modeling techniques mentioned above:

- *Multiple function types* - It allows to deal with various types of parametric functions. By using a library of shapes, more accurate estimates are performed compared to classical approaches such as the Gaussian mixture one [11].

- *Lidar physical knowledge integration* - Complex prior information on lidar waveform characteristics can be introduced in the energy without having problems of convexity or/and continuity restrictions in the formulation of these interactions.

- *Efficient exploration of configuration spaces* - A RJMCMC sampler with relevant proposition kernels allows to avoid exhaustive explorations of continuous configuration spaces, and is particularly efficient when the number of functions is unknown. Generally speaking, the MCMC samplers offer good potentialities in signal reconstruction [12], and for instance in lidar waveform estimate for counting and locating the reflected returns from surfaces [13].

The proposed model is formulated in Section 2. Section 3 describes the optimization procedure. Results are then shown in Section 4 as well as 3D point clouds generated from our approach. Finally, conclusions and perspectives are drawn.

2. MODEL DEFINITION

2.1. Marked point processes

A marked point process in $S = K \times M$ is a point process living in a continuous bounded set K supporting a 1D-signal where each point is associated with a mark specifying an object [6]. In our method, each lidar waveform is modeled by a marked point process with $K =$

$[0, \mathcal{N}_{\max}]$, where \mathcal{N}_{\max} is the size of the waveform and M , the mark space. The objects of the process are parametric functions taken from a predefined library. They are described by a certain number of random variables corresponding to their parameters. The marked point process is specified by a density function $f(\cdot)$ w.r.t a measure of reference (*i.e.*, the Poisson measure). This density, which allows to take into account complex interactions between objects, is usually expressed using a Gibbs energy $U(\cdot)$ (*i.e.*, $f \propto \exp -U$). In order to find the configuration x of functions that better fits the waveforms, we estimate the global minimum of U by coupling a MCMC sampler with a simulated annealing.

2.2. Library of modelling functions

The contents of the library is a key point since the function parameters will be used afterwards for classifying 3D point clouds. The Generalized Gaussian (GG) model has been shown to fit most of the echoes of lidar waveforms in urban areas [2]. Nevertheless, this assumption is not always sufficient and new functions are introduced both to fit asymmetric echoes (echoes are slightly distorted by roof materials and ground surface) and symmetric ones but with other parameters than those provided by the GG model. For instance, the GG model gives the amplitude and width for symmetric echoes whereas the Weibull distribution provides a scale and a shape parameter and the Burr one simulates asymmetric modes (*cf.* Table 1).

2.3. Energy formulation

Let x be a configuration of parametric functions (or objects) x_i extracted from the above library. The energy $U(x)$ measuring the quality of x is composed of both a data term $U_d(x)$ and a regularization one $U_p(x)$ such as:

$$U(x) = \beta U_d(x) + (1 - \beta) U_p(x) \quad (1)$$

where $\beta \in [0, 1]$ tunes the trade-off between the prior energy and the data term.

2.3.1. Data energy

The data energy helps the model to best fit to the lidar waveforms. The likelihood can then be obtained by computing a distance between the given signal $\mathcal{S}_{\text{data}}$ and the estimated one $\hat{\mathcal{S}}$, which depends on the current objects on the configuration x .

$$U_d(x) = \sqrt{\frac{1}{|K|} \int_K (\hat{\mathcal{S}} - \mathcal{S}_{\text{data}})^2} \quad (2)$$

This term, which measures the quadratic error between both signals, allows to be sensitive to high variations *i.e.*, to local strong errors in signal estimate.

2.3.2. Prior energy

$U_p(x)$ allows to introduce interactions between objects of x , and to favor/penalize some configurations. For aerial lidar waveforms, the prior knowledge is set up by physical limitations in the backscatter of lidar pulses.

$$U_p(x) = U_n(x) + U_e(x) + \sum_{x_i \sim x_j} U_m(x_i, x_j) \quad (3)$$

where $x_i \sim x_j$ constitutes the set of neighboring objects in the configuration x . This neighborhood relationship \sim is defined as follow:

$$x_i \sim x_j = \{(x_i, x_j) \in x \mid |\mu_{x_i} - \mu_{x_j}| \leq r\} \quad (4)$$

μ_{x_i} (*resp.* μ_{x_j}) represents the mode (*i.e.*, the position of the maximum amplitude of the echo) of the associated function to object x_i (*resp.* x_j), and r is the lidar sensor range resolution (*i.e.*, the minimum distance between two objects along the laser line of sight that can be differentiated).

(i) Echo number limitation The two first echoes of a waveform contain in general about 90% of the total reflected signal power. Consequently, even for complex targets like forested areas, a waveform empirically reaches a maximum of seven echoes and it is quite rare to find more than four echoes. In urban areas, most of the targets are rigid, opaque structures like buildings and streets. Thus, more than two echoes are usually found in non dense trees. We then aim to favor configurations with a limited number of objects with an energy given by:

$$U_n(x) = -\log P_{\text{card}(x)} \quad \text{with} \quad \sum_{n=0}^{\infty} P_n = 1 \quad (5)$$

where P_n is the probability for the waveform to have n echoes. The probabilities are empirically set up by a coarse mode estimate on a urban test area. Here, we have: $P_1 = 0.6$, $P_2 = 0.27$, $P_3 = 0.1$ and $P_{4 \leq n \leq 7} = 0.01$. For $n > 7$, $U_n(x)$ is set to a positive hardcore value.

(ii) Backscattered energy limitation As an airborne laser system cannot physically receive a signal with an higher energy than emitted, it is possible to formulate a backscattered energy based on this property.

$$U_e(x) = \omega_e \mathbb{1}_{\{E(x) > E_{\text{ref}}\}} (E(x) - E_{\text{ref}})^2 \quad (6)$$

where $\mathbb{1}_{\{\cdot\}}$ is the characteristic function, $E(x) = \int_K \mathcal{S}_x$ is the energy of the configuration x , compared to a reference power E_{ref} , set with the knowledge of the emitted lidar power. Only waveforms with superior energy are penalized: no assumption can be formulated on the received energy since it depends on the target properties.

(iii) Sensor range resolution limitation We aim to penalize objects spatially closer along the line of sight than the sensor range resolution. Such energy is given by:

$$U_m(x_i, x_j) = \omega_m \exp \left(\frac{r^2 - |\mu_{x_i} - \mu_{x_j}|^2}{\sigma^2} \right) \quad (7)$$

and also permits to favor configurations with a small number of objects. Indeed, a single pulse can be fitted by an important number of echoes but such situation does not reflect the reality.

2.3.3. Parameter settings

Physical and weight parameters can be distinguished. Physical parameters are r and σ . We choose $\sigma = 0.01$ ns and $r = 5$ ns. Data and regularizing terms are weighted one compared to the other, respectively with a factor β set to 0.5. The two prior weights are tuned by “trial-and-error” tests.

3. OPTIMIZATION

We aim to find the configuration of objects which minimizes the non convex energy U in a variable dimension space since the number of objects is unknown and function types are defined by different number of parameters. Such a space can be efficiently explored using a Reversible Jump Markov Chain Monte Carlo (RJMCMC) sampler

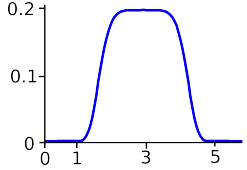
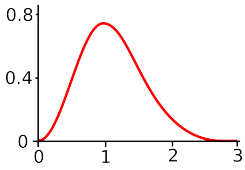
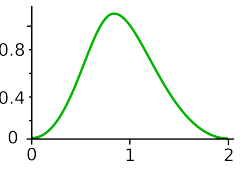
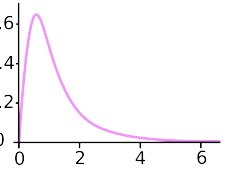
Model	Generalized Gaussian	Weibull	Nakagami	Burr
Parameters	I, s, σ, α	I, s, k, λ	I, s, μ, ω	I, s, a, b, c
Specificity	typically used	asymmetric, new parameters	skewness parameter	2 shape parameters
Shape	 $I=1, s=3, \sigma=2, \alpha=3$	 $I=1, s=0, k=2, \lambda=1$	 $I=1, s=0, \mu=2, \omega=1$	 $I=1, s=0, a=1, b=2, c=1$

Table 1. Library of models. I and s are common parameters to all functions, respectively for amplitude and shift or location.

coupled with a simulated annealing.

The RJMCMC sampler [10] consists in simulating a discrete Markov Chain (X_t), $t \in \mathbb{N}$ on the configuration space, having an invariant measure specified by the energy U . This sampler performs "jumps" between spaces of different dimensions respecting the reversibility assumption of the chain. One of the advantage of this iterative algorithm is that it does not depend on the initial state. The jumps are realized according to three kinds of move called proposition kernels:

- **Perturbation kernel:** the parameters of an object belonging to the current configuration x is modified;
- **Birth-and-death kernel:** an object is added or removed from the current configuration x and
- **Switching kernel:** the type of an object belonging to x is switched with another type of the library.

The probabilities of choosing each move are equal since no assumption can be made on which move is more relevant at the current state.

A simulated annealing is used to ensure the convergence process. A relaxation parameter T_t , defined by a sequence of temperatures decreasing to zero when $t \rightarrow \infty$, is introduced in the RJMCMC sampler (*i.e.*, $U(\cdot)$ is substituted by $\frac{U(\cdot)}{T_t}$). The simulated annealing allows to theoretically ensure the convergence to the global optimum for all initial configuration x_0 using a logarithmic temperature decrease. In practice, we prefer using a geometrical cooling scheme which is faster and gives an approximate solution close to the optimal one. During the temperature decrease, the process explores the configurations of interest and becomes more and more selective. It corresponds to local adjustments of the object of the configuration. To sum up the optimization process, if at t , $X_t = x$

1. Choose randomly one of the proposition kernel Q_i ;
2. According to Q_i , choose a new configuration y from x ;
3. Take $X_{t+1} = y$ with a probability
$$\min \left[1, \frac{Q_i(y \rightarrow x)}{Q_i(x \rightarrow y)} \exp - \left(\frac{U(y) - U(x)}{T_t} \right) \right]$$
 and take $X_{t+1} = x$ otherwise.

4. RESULTS

4.1. Experiments on simulated signals

To assess the reliability of the algorithm, it has been first applied on signals with a higher complexity than real lidar waveforms. Longer signals with more echoes than physically expected, with distorted and overlapping modes as well as corrupted with noise have been

fitted with our method. One just has to tune the prior physical parameters to extend the energetical formulation to other kinds of signals. To deal respectively with very close echoes and with large overlapping ones, the interaction between objects can be changed by decreasing and increasing r and σ . To reconstruct signals with higher energy, E_{ref} can be tuned. To fit signals with more modes, the echo number limitation can be modified by accepting more echoes within the signal and with the same probability.

Figure 2 shows that good fitting results can be achieved on simulated waveforms, even corrupted with Gaussian noise, by tuning prior parameters, assessing the reliability of the algorithm on 1D random signals. The nine echo locations are accurately found. However, small differences between the reference and the estimated signals can be locally noticed, especially with noisy signals where the algorithm has more difficulties to find the exact maxima and fit the upper parts of the modes (*e.g.*, 2nd and 4th echoes in Figure 2b).

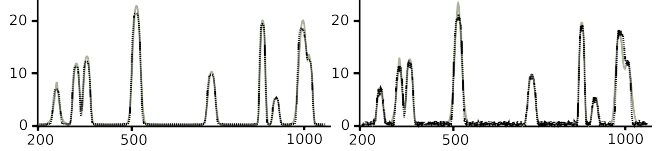


Fig. 2. Results of complex waveform fitting on a simulated signal with nine echoes (**left**) and on the same signal with Gaussian noise (**right**). The dotted black line and the continuous grey one are respectively the raw and the reconstructed signals.

4.2. Airborne lidar waveforms

Waveforms acquired from an airborne lidar system over different kinds of landscapes have been analysed using the marked point process approach. Figure 4 shows results both on urban (buildings) and natural (trees, hedges) items. The right number of echoes is found as well as the correct shape of the waveform: single and multiple overlapping echoes are retrieved, even in vegetated areas where the noise level is significant w.r.t. the echo amplitudes (Figures 4c and d).

The Generalized Gaussian, Weibull and Nakagami functions have been introduced to model the same kind of echoes. Thus, there is no concluding whether the minimal configurations obtained are composed of the right modeling functions. As expected, the Burr model allows to fit slightly asymmetric echoes, especially the second echo of two overlapping ones (Figures 4b, d and f).

Approximatively 80000 waveforms have been fitted over a urban

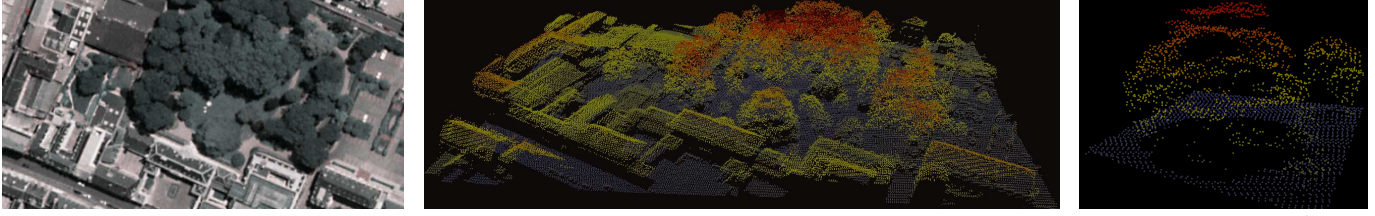


Fig. 3. Results of waveform decomposition on a urban area with dense trees and complex buildings. **Left:** orthoimage of the test area © IGN. **Middle:** resulting 3D point cloud (Blue: low elevation → brown: high elevation) over the whole area. **Right:** results over two trees showing that points inside tree canopy are retrieved.

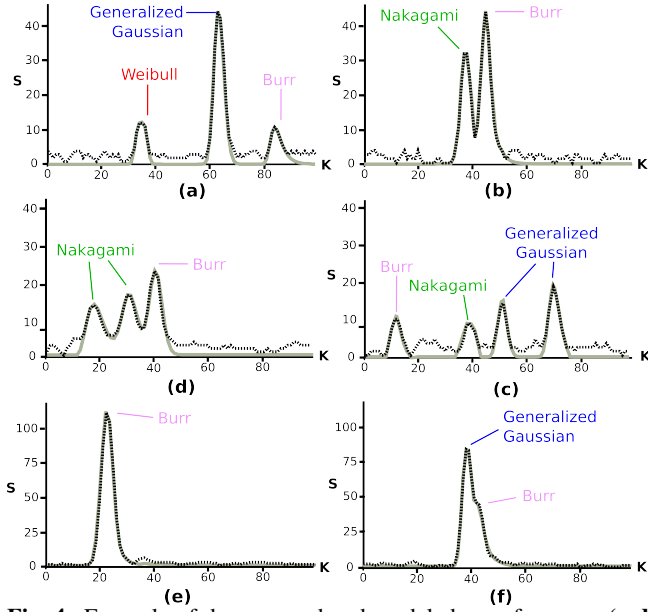


Fig. 4. Example of decomposed and modeled waveforms on (a-d) trees, (e) a building roof and (f) a hedge.

area to assess the reliability of the method in a complex and heterogeneous landscape. A waveform-by-waveform evaluation of the fitting process to estimate the correctness of the echo detection would be highly time-consuming. Thus, the algorithm has been rather evaluated by computing the relative amplitude error ε on each signal with the L_∞ norm to detect missing echoes. For that purpose, the noise within raw signals is first removed. Finally, the mean error computed on 80000 signals is $\varepsilon=4.1\%$: the ground and buildings waveforms are fitted with lower amplitude error ($\varepsilon_a=3.4\%$) than vegetation ones ($\varepsilon_v=7.9\%$). The weak difference between ε_a and ε_v can be explained by the fact that waveforms over vegetated areas have much more complex shapes than over anthropic surfaces but have much lower amplitudes (see Figure 4).

The waveform decomposition allows to retrieve the mode of each echo which corresponds to the range between the sensor and a target. The 3D cartographic coordinates of each echo can then be computed from the range values using georeferencing formulas. Figure 3 displays the resulting 3D point cloud of this process over the test area, which can be now classified using the estimated parameters of modeling functions as performed in [2].

5. CONCLUSION AND FUTURE WORKS

We have proposed an original method for modeling airborne lidar waveform by complex parametric functions. The obtained results are satisfactory. The proposed marked point process approach is well adapted both to locate echoes in signals and accurately describe them with parametric functions. 3D points can therefore be generated over large areas with echo shape descriptors taken from the

extensible model library and offer the possibility to improve classical lidar point cloud classification algorithm. Moreover the physical parameters of the proposed energy are tunable and offer the possibility to extend the method to other kinds of signals and lidar sensors (terrestrial and spatial).

Finally, in future works, it would be interesting to estimate automatically the weighting parameters using for instance the *Expectation-Maximization* algorithm. Moreover, we should introduce in the energy formulation specific interactions between parametric functions of different types in order to improve local signal adjustments.

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